

# Energy Demand and Trading Optimization in Isolated Microgrids

Richard Chidzonga  
Department of Electronic Engineering  
Durban University of Technology  
Durban, South Africa  
RCFoya@mut.ac.za

Masimba Gomba  
Department of Electronic Engineering  
Durban University of Technology  
Durban, South Africa  
massyngomba@gmail.com

Bakhe Nleya  
Dept of Electronic Eng  
DUT  
Durban, South Africa  
bakhen@dut.ac.za

**Abstract**—Future generation or smart grid (SG) will incorporate ICT technologies as well as innovative ideas for advanced integrated and automated power systems. The bidirectional information and energy flows within the envisaged advanced SG together with other aiding devices and objects, promote a new vision to energy supply and demand response. Meanwhile, the gradual shift to the next generation fully fledged SGs will be preceded by individual isolated microgrids voluntarily collaborating in the managing of all the available energy resources within their control to achieve optimality in both demand and distribution. In so doing, innovative applications will emerge that will bring numerous benefits as well as challenges in the SG. This paper introduces a power management approach that is geared towards optimizing power distribution, trading, as well as storage among cooperative microgrids (MGs). The initial task is to formulate the problem as a convex optimization problem and ultimately decompose it into a formulation that jointly considers user utility as well as factors such as MG load variance and associated transmission costs. It is deduced from obtained analytical results that the formulated generic optimization algorithm characterizing both overall demand and response by the cooperative microgrids assist greatly in determining the required resources hence leading to cost effectiveness of the entire system.

**Keywords**—energy cooperative microgrids, energy storage system, smart grid

## I. INTRODUCTION

As the existing electrical power system infrastructures are fast approaching their rated capacities, next generation SGs become a viable alternative as well as ultimate solution. The key components of SGs, such as advanced metering infrastructure (AMI) and renewable energy generating resources, have resulted in a demand for the devising of new grid management approaches. Typically, the bidirectional operation of next generation SGs as well as high renewable energy integration has the potential to enhance the overall stability of the grid in terms of demand and supply. Renewable energy integration implies ‘random’ injection of renewable energy resources into the existing power grid and this will certainly complicate the overall energy management. This is partly because renewable energy sources produce output power (peak) in unpredictable ways as wind or sunlight strengths will vary from time to time, thus making it difficult for any network operator to rely on them for balancing supply and demand. Overall, various issues related to the integrating of the renewable resources into a grid emerge. These include voltage stability, power factor quality, harmonics, devices protection and overall power grid system reliability. With regards to voltage stability, it is generally noted that as the number of distributed generations increase,

so will be the number and capacities of energy storage systems (ESSs). The latter has the potential to reduce the uncertainty as well as fluctuations associated with distributed generation and thus the rated grid’s voltage/frequency profiles can be stabilized. However, on-lining of a single distributed generator may immediately trigger localized load, voltage, frequency control fluctuations.

It is also necessary that all SG devices be monitored in real time, hence the necessitation of advanced information and communications technology (ICT) subsystem infrastructures to facilitate reliable connectivity as well as secured connectivity. In this case, the efficiency as well as both physical and semantic security of the ICT subsystem are imperative. It is generally agreed that computational efficiency in the energy management of an SG is key to its successful operation.



Fig. 1. Key SG Components.

A typical SG and its components are illustrated in Fig. 1. It basically comprises smart power and ICT subsystems. Smart power system refers to a reliable as well as an intelligent power system which comprises distributed power generation, transmission, distribution, as well as storage (ESSs) components. The ICT subsystem facilitates advanced metering, smart monitoring, and the corresponding information management. The ICT subsystem will also facilitate the implementation of key SG applications relating to energy management, system reliability, security and privacy. Other emerging applications include energy management for large-scale support of electric vehicles (EV) and distributed generation of renewable energy in MGs.

Overall, key to the successful operation of SG (or at MG level), is the implementation of demand-side management [1] [2]. The inclusion of renewable generation means overall demand and generation within the cooperating SGs is facilitated and addressed by multitudes of sources sparsely located within the SG, and at multiple timescales. This same information will be used to shift peak load and peak hours utilizing distributed optimization, as well as ultimately preventing peak loading on the SG system. Individual users are also able to embark on their own home demand side energy management by shifting electricity consumption of high energy usage appliances to off-peak hours. Smart enabled user appliances could be selectively put off during peak hour demand as well as concurrently execute intelligent strategies to shift energy consumption to non-peak hours [3].

In [4], the authors looked at energy demand scheduling modeling for an individual user (residential) energy management. Using the game-based theory approach, the authors attempt to solve the game model via the best response dynamics. With this approach energy usage related data is exchanged among participating SG customers in an attempt to reduce the overall average peak to average energy usage ratios. This approach is further explored [5] where the focus is on further minimizing the average peak to average energy usage ratios. This paper will focus on addressing allocation issues under the context of cooperating microgrids as we evolve towards fully fledged smart grids.

## II. RELATED WORKS REVIEW

Key to the optimal power demand and supply in that MG would be in its capability to provide the power to all households within its vicinity on demand. Due to the intermittency nature of renewable generation, quite often some neighboring MGs might have excess generation and storage capacities compared to others. It is therefore worthwhile for neighboring MGs to operate in a cooperative manner by interconnecting and sharing the available power and generating/storage resources.

As a result of the cooperative association between the MGs, the problem of customer demand-side management arises. This is because the cooperative MGs ought to optimally operate to the satisfaction of all participating users. The resulting residential demand-side management problem can thus be modeled as having constraints that are focused on relieving users from any inconveniences associated with the modeling itself. It is also necessary to address an appropriate trading model for microgrid operations, where a risk-free optimal trading strategy can be devised as well as optimization of resources taking into consideration the uncertainties of power generation levels from time to time.

Lots of past and current research work has focused on the energy trading problem in cooperative MGs. The traditional power grid is always included in the energy trading market. Further advancements in renewable technology [6] have provided an impetus for creating MGs with affordable multiple distributed energy conversions. Since demand and generation problem arises from a multitude of sources and at various timescales in MG-based energy trading markets, new distributed optimization and control solution approach-

es as well as technologies are necessary to further reduce OPEX as well as CAPEX, thus ultimately driving towards more economical and environmental benefits with regards to next generation smart grids. These approaches and technologies pose the potential to bring about a reduction in the intermittency of renewable energy by way of implementing various proactive demand response programs.

The authors in [7],[8] and [9] studied a distributed optimization framework for the energy trading amongst islanded MGs. A linear supply bidding function-based demand response program is proposed in [10] whereby an operator collects the bids and capacities from each user and utilizes them to achieve some form of competitive equilibrium. In [11] and [12] the researchers proposed and analyzed a multi-layer energy trading market for electric vehicles in which the trading price and the quantity of the energy to trade was determined using some form of a proposed double auction mechanism. In all the works mentioned herein, the general intermittency of renewable energy coupled with demand uncertainties were never considered. The two exposes the system's reliability to vulnerability. Therefore, it may be necessary to use both stochastic and probabilistic measures to solve the problem as it is random in nature. The authors in [13] introduced a dynamical model with certain probabilistic transitions which can be played by one or more players. The proposed energy trading model incorporates the day-ahead as well as real-time markets.

This paper explores real-time energy demand and the supply management problem for cooperative MGs. We assume that each individual microgrid controller (MC) intends to serve its users with full satisfaction, as well as sustainability of the available RDG systems. Each MC may consist of several RDG as well as a centralized ESS system. Power demand and supply within each MC is coordinated as well as facilitated by a dedicated in-house MG control center (MGCC). An external control center (MaGCC) coordinates both power exchanges between the two cooperative MCs as well as power trading.

## III. USER POWER USAGE MODELLING

We consider a system of cooperative MGs which trade as well as exchange power via a commonly shared power bus. The RDG are taken as the main sources and the utility as a back-up. For greater microgrid autonomy, an ESS (Energy Storage System) is built into the model. The later stores excess generated energy and supplies the loads when RDG local energy is insufficient. In the off-grid mode, the ESS is acts as the backup supply for energy balancing.

### A. Model Definitions

We assume that a standard user has  $n \in \{1, \dots, N\}$  household appliances. Their power usage is modeled hourly over a 24 hour period. The power usage matrix,  $[A_n]_{N \times 24}$  is defined by  $R_n$  rows representing respective appliances' energy usage curves and corresponding  $T$  (fixed time intervals) columns characterizing each of the  $t \in \{1, \dots, T\}$  appliances. We can use the defined matrix to determine power usage by  $N$  ag-

gregate appliances the at any arbitrary time  $t$  as being equal to:

$$a(t) = \sum_{n=1}^N a_n^{\alpha_n}(t) \quad (1)$$

Where  $a_n^{\alpha}(t)$  is an element of  $[A_n]_{N \times 24}$ , a row  $\alpha \in [1, \dots, R_n]$  and corresponding column  $t \in [1, \dots, T]$  such that  $T = 24$  hours. We can further go on to elaborate on factors such as cost benefit as well as power generation costs linked to the user's  $n \in \{1, \dots, N\}$  appliances. If the user owns a total of  $M$ ,  $n \in \{1, \dots, M\}$  RDG sources the  $n^{\text{th}}$  with capacity  $g_n$ , then the corresponding aggregated generation capacity is:

$$g(t) = g_1 + g_2 + \dots + g_M = g^l(t) + g^E(t) = \sum_{n=1}^M g_n(t) \quad (2)$$

The renewable generated power,  $g(t)$  comprises a fraction that is utilized in-house  $g^l(t)$  and the traded component  $g^E(t)$ . Let  $p_a(t)$  and represent the unit cost of RDG power traded between users linked in the microgrid and  $p_g(t)$  a similar quantity for power sold by the utility grid. Consequently, the corresponding cost of generation in  $n \in \{1, \dots, N\}$  incurred by the user is:

$$aC(t) = \sum_{n=1}^M c_n(g_n(t)) \quad (3)$$

### B. Consumer level Optimization Formulation

The incentive to the consumer is captured by a real valued function that summarizes the consumer's objectives. This objective function is generally formulated as the difference between the the utility accrued to the consumer less all costs incurred, (4).

$$Utility = Benefit - Cost \quad (4)$$

$D(t)$  is the net demand of the consumer less internal generation component, (5). At each hour the state of the system is defined by  $D(t), P_a(t), P_g(t)$  and ESS state of charge,  $S(t)$ . Considering equations (1), (2) and (3) and objective function characterizing the user's power usage is expressed as:

$$D(t) = \left( \sum_{n=1}^N a_n^{\alpha_n}(t) \right) - g^l(t) \quad (5)$$

$$f = \sum_{n=1}^N d_n^{\alpha_n} + \sum_{t=1}^T p_g(t) \cdot g^E(t) - \sum_{t=1}^T p_a(t) \cdot D(t) - \sum_{n=1}^M c_n(g_n(t)) \quad (6)$$

Where  $d_n^{\alpha}$  a cash equivalent benefits and  $c_n(g_n)$  - is a unit cost of generating power. The ultimate objective is to ensure that there is always more power traded to the grid to maximize the utility to consumer;

$$g^E(t) \leq g(t) = \sum_{n=1}^M g_n(t) \quad (7)$$

From (6) it also follows that for a user trading all his/her own generated power by, i.e.  $g^E(t) = g(t)$  we have;

$$f = \sum_{n=1}^N \sum_{t=1}^T \left[ \frac{d_n^{\alpha_n}}{T} - p(t) a_n^{\alpha_n}(t) \right] + \sum_{n=1}^M \sum_{t=1}^T [p_g(t) \cdot g_n(t) - c_n(g_n(t))] \quad (8)$$

Our objective would be to maximize;

$$f = \sum_{n=1}^M \sum_{t=1}^T [p_g(t) \times g_n(t) - c_n(g_n(t))] \quad (9)$$

### IV. POWER SCHEDULING BETWEEN MGs

An example of power storage sharing among cooperative MGs is depicted in Fig. 2. As shown, three MGs with storage (ESS) are interconnected. We assume that power during charging of  $ESS_i$  is  $C_i \geq 0$  at a charging efficiency  $\eta_i^c$  such that  $0 \leq \eta_i^c < 1$ . Similarly discharging rate of the ESS is  $D_i$  such that  $D_i \geq 0$ , with discharging efficiency is  $0 \leq \eta_i^d < 1$ .

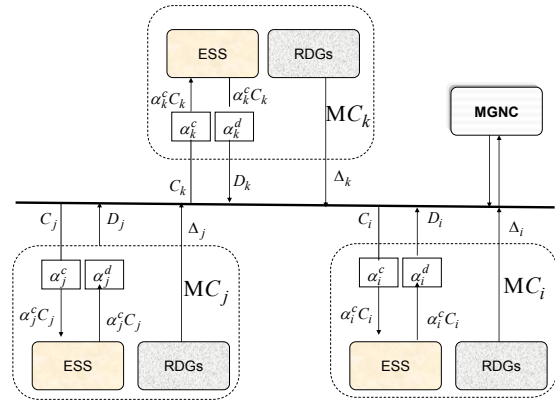


Fig. 2. Energy transfer model of system

The storage capacity of  $ESS_i$  is;

$$S_{i+1} = S_i + \eta_i^c C_i - \frac{D_i}{\eta_i^d} \quad (10)$$

$$f = s_{i,\min} = S_i + \eta_i^c \sum_{k=1}^i C_k - \frac{1}{\eta_i^d} \sum_{k=1}^i D_k \leq S_{i,\max} \quad (11)$$

The constraint on the power storage levels would be given by:

$$s_i'(t) = s_i(t) - \xi ; s_i(t-1) \quad (12)$$

$$s_{i,\min} \leq s_i(t) \leq s_{i,\max} , \forall i \in i, j, k \quad (13)$$

$$\frac{s_{m,\min}}{(1-\xi)} - s_{m,\max} \leq s_m'(t) \leq s_{m,\max} - s_{m,\min} \quad (14)$$

## V. LOAD PREDICTIONS

To further enhance the demand and supply optimization among cooperative MGs, load predictions may be done with the aid of a neural network (NN) set. In this case, we forecast tomorrow's load (load T) by using load demand curves obtained an hour earlier, (T-1), day before (T-24) and one week ago (T-168). [14], [15]. The next day load forecasting is then conducted hour by hour. The next hour forecasting is based on the prediction of previous one. The authors in [14] also incorporated various factors that could affect power generation and usage. These included weathers, season, as well as economic factors [14]. Under weather factors, elements such as temperature humidity index (THI), dry bulb temperature (DBT), wind chill index (WCI) and wet bulb temperature (WBT) are considered.

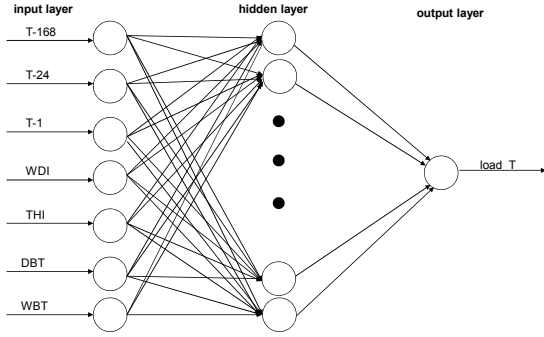


Fig. 3. Tomorrow's load forecasting using NNs

The ANN is trained by back propagation whereby the output is produced by presenting input training data to the network. The error between the net output and target output network weights ( $\omega_{ij}$ ) are adjusted to reduce the output error. The advantage in the use of artificial NNs (ANNs) in load forecasting is in that it does not require assumption of any direct mappings between load and climatic variables in the necessary non-linear modeling and adaptation associated with the load prediction process. The next day load is determined by way of iterative forecasting method explained in [16]. As shown in Fig. 3, the ANN network comprises three layers; input, hidden (middle) as well as the output layer. The hidden layer is key in ensuring the balance of model flexibility as well as over-fitting. A sigmoid function is used for activation.

## VI. ANALYSIS

We first compare two ESS charging approaches namely:

- Linear Supply Function Based Pricing, which relates to a linear supply function-based pricing method applied to dynamically adjust the charging strategy according to the different levels of the charging.
- Charging Strategy by Stochastic Game, where in this case, the additional charging load may affect the lifespan or failure of the charging transformer hence that risk is considered.

In this section, we evaluate the two-stage stochastic game approach on the energy management studied. The data used

for the analysis is obtained from both [17] and [18]. Key climatic data such as solar intensities, wind availability speed, humidity and daily average temperatures are also derived from the same sources. The data is normalized over a 24-hour period, i.e. corresponding to a full day with hourly intervals  $\Delta t = 1$  for case study purposes.

Table 1. Parameters of a typical CHP system

NO	$DR$	$Q_{max}$	$UR$	$\eta$
1	680	1300	680	45
2	680	1288	680	45

\*\*  $DR$ ,  $Q_{max}$  and  $UR$  are measured in  $kWh$

The predictive excess power output of 4 MGs: namely, CHP, Wind, PV and DR based is provided in Fig. 4. It is noted that the wind in the areas chosen has a relatively greater degree of fluctuations as well as uncertainty.

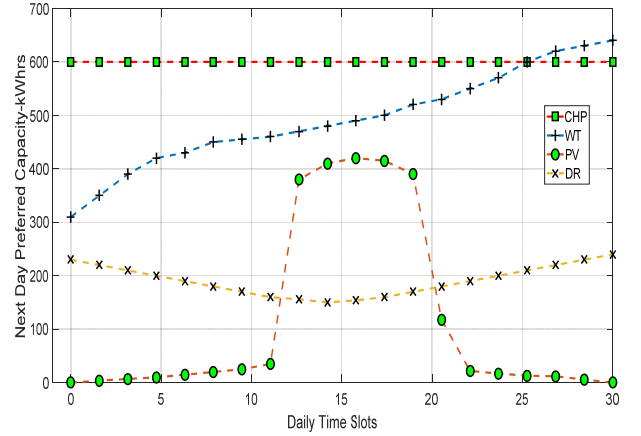


Fig 4. Predictive power output for 4 MGs

We further go on to explore an optimal ESS storage capacity required for each MG. Each MG charges its ESS when available grid power is priced lowest and discharges when the cost escalates. Each charge controller is rated at approximately 20% of the ESS capacity in (Ahs). In practice, the charging will take much longer because of the excessive losses (typically up to 40%) involved.

Table 2. Example Specifications

ELECTRICAL STORAGE SYSTEM		MG LINE RATINGS	
$\eta_i^c$	0.8		
$\eta_i^d$	0.8	$R(\text{type I})$	0.1 $\Omega/km$
$S_i$	0.01	$R(\text{type II})$	0.3 $\Omega/km$
$S_i^{\min}$	0.01	$d$	55km
$S_i^{\max}$	70 MW	$V$	33kV
$S_j^{\max}$	90 MW	$E$	50MW
$S_k^{\max}$	110 MW	$T^\circ$	$0^\circ - 28^\circ \text{ max}$

Listed in the above table (Table 2) are the main electrical specifications of the ESS system as well as key power grid transmission line parameters.

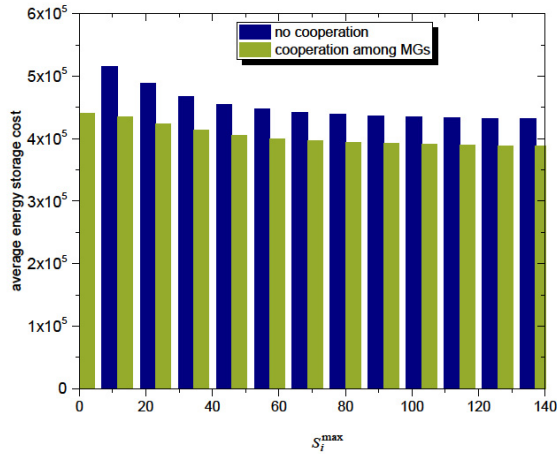


Fig. 5. Power cost versus required ESS capacity.

An analytical plot of the total power cost versus the available ESS in the MGs is provided in Fig. 5 in which it is ascertained that total energy cost is achieved with a relatively lower value of  $S_i^{\max}$ .

## VII. CONCLUSION

This paper has looked at energy management for cooperative microgrids. The user energy management problem was formulated as a practical MILP optimization problem to minimize the total system cost including those of the MGs. The initial task was to formulate the problem as a convex optimization problem and ultimately decompose it into a formulation that jointly takes into account user utility as well as MG load variance and transmission costs. It is deduced from obtained analytical results that the formulated generic optimization algorithm characterizing both aggregated demand and response from the cooperative MGs assist greatly in the determination of optimal resources (in terms of quantity) to enable operational cost viability of entire system

This work can be further extended in two directions. Firstly, by considering the intermittency of renewable generation and random demand, for which the current deterministic methods are not adequate. Secondly, investigation of trading mechanisms such as employing pricing to supporting SG grid networks and encourage energy sharing in a cluster of MGs.

## REFERENCES

- [1] [1] P. Palensky and D. Dietrich, "Demand side management: Demand response, intelligent energy systems, and smart loads," *IEEE Transactions on Industrial Informatics*, vol. 7, no. 3, pp. 381–388, 2011.
- [2] X. Yu, C. Cecati, T. Dillon, and M. G. Simoes, "The new frontier of smart grids," *IEEE Industrial Electronics Magazine*, vol. 5, no. 3, pp. 49–63, 2011.
- [3] A.-H. Mohsenian-Rad, V. W. Wong, J. Jatskevich, R. Schober, and A. Leon-Garcia, "Autonomous demand-side management based on game-theoretic energy consumption scheduling for the future smart grid," *IEEE Transactions on Smart Grid*, vol. 1, no. 3, pp. 320–331, 2010.
- [4] B.-G. Kim, S. Ren, M. van der Schaar, and J.-W. Lee, "Bidirectional energy trading and residential load scheduling with electric vehicles in the smart grid," *IEEE Journal on Selected Areas in Communications*, vol. 31, no. 7, pp. 1219–1234, 2013.
- [5] C. Joe-Wong, S. Sen, S. Ha, and M. Chiang, "Optimized day-ahead pricing for smart grids with device-specific scheduling flexibility," *IEEE Journal on Selected Areas in Communications*, vol. 30, no. 6, pp. 1075–1085, 2012.
- [6] M. R. Singh, E. L. Clark, and A. T. Bell, "Thermodynamic and achievable efficiencies for solar-driven electrochemical reduction of carbon dioxide to transportation fuels," *Proceedings of the National Academy of Sciences*, vol. 112, no. 45, pp. 6111–6118, 2015.
- [7] A.-H. Mohsenian-Rad, V. W. Wong, J. Jatskevich, R. Schober, and A. Leon-Garcia, "Autonomous demand-side management based on game-theoretic energy consumption scheduling for the future smart grid," *IEEE Transactions on Smart Grid*, vol. 1, no. 3, pp. 320–331, 2010.
- [8] D. Gregoratti and J. Matamoros, "Distributed energy trading: the multiple-microgrid case," *IEEE Transactions on Industrial Electronics*, vol. 62, no. 4, pp. 2551–2559, 2015.
- [9] C. Li, X. Yu, W. Yu, and T. Huang, "Networked optimization for demand side management based on non-cooperative game," in 2015 IEEE 13th International Conference on Industrial Informatics (INDIN). IEEE, 2015, pp. 1159–1164.
- [10] [ Y. Xu, N. Li, and S. H. Low, "Demand response with capacity constrained supply function bidding," *IEEE Transactions on Power Systems*, vol. 31, no. 2, pp. 1377–1394, 2016.
- [11] A. Y. Lam, L. Huang, A. Silva, and W. Saad, "A multi-layer market for vehicle-to-grid energy trading in the smart grid," in 2012 IEEE Conference on Computer Communications Workshops (INFOCOM WKSHPS). IEEE, 2012, pp. 85–90.
- [12] Y. Wang, W. Saad, Z. Han, H. V. Poor, and T. Bassar, "A game-theoretic approach to energy trading in the smart grid," *IEEE Transactions on Smart Grid*, vol. 5, no. 3, pp. 1439–1450, 2014.
- [13] L. S. Shapley, "Stochastic games," *Proceedings of the National Academy of Sciences*, vol. 39, no. 10, pp. 1095–1100, 1953.
- [14] A. D. Papalexopoulos, S. Hao, and T.-M. Peng, "An implementation of a neural network based load forecasting model for the ems," *IEEE Transactions on Power Systems*, vol. 9, no. 4, pp. 1956–1962, 1994.
- [15] A. AlFuhaid, M. El-Sayed, and M. Mahmoud, "Cascaded artificial neural networks for short-term load forecasting," *IEEE Transactions on Power Systems*, vol. 12, no. 4, pp. 1524–1529, 1997.
- [16] A.R. Reis and A. A. da Silva, "Feature extraction via multiresolution analysis for short-term load forecasting," *IEEE Transactions on Power Systems*, vol. 20, no. 1, pp. 189–198, 2005.
- [17] <https://energyexemplar.com/wp-content/uploads/AEMO-Observations-Operational-and-Market-Challenges-to-Reliability-and-Security-in-NEM.pdf>.
- [18] L. Foster, Wagner, A. Liebman, "Modelling the Electricity and Natural Gas Sectors for the Future Grid: Developing Co-Optimisation Platforms for Market Redesign", August 1, 2016. [https://mpr.ub.uni-muenchen.de/70114/1/MPRA\\_paper\\_70114.pdf](https://mpr.ub.uni-muenchen.de/70114/1/MPRA_paper_70114.pdf).